

THE SCIENCE AND PRACTICE OF EROSION THRESHOLD THEORY

in Applied Geomorphology



Roger TJ Phillips and Peter Ashmore



Erosion Threshold Awareness

The Science

- Boundary types and sediment **mixtures**
- The good ol' **Shields** parameter
- Don't be scared of **selective** mobility

The Practice

What **sometimes** works, sort of, maybe...)

- Threshold versus **alluvial** channel beds
- Factors of **safety**
- **Uncertainty**, does it matter?
- Field **verification** of erosion thresholds





CONTINUUM OF CHANNEL BOUNDARY TYPES

SAND



GRAVEL



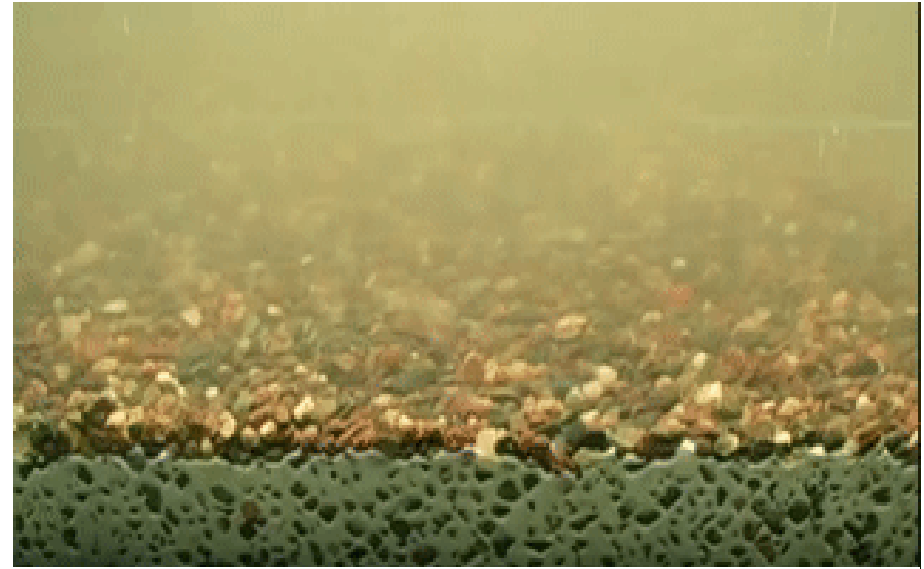
CLAY



COBBLE



Bedload Transport of Sediment Mixtures



Credit: John Gaffney (2009) University of Minnesota Department of Civil Engineering St. Anthony Falls Lab

EROSION THRESHOLDS SEDIMENT MOTION

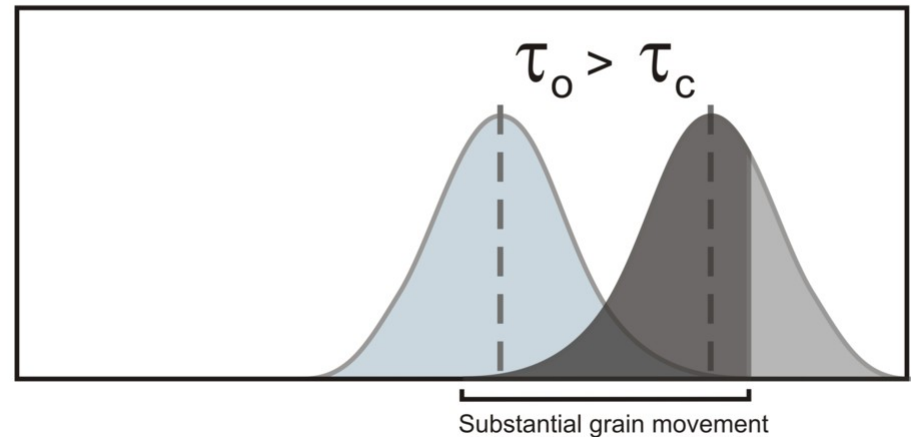
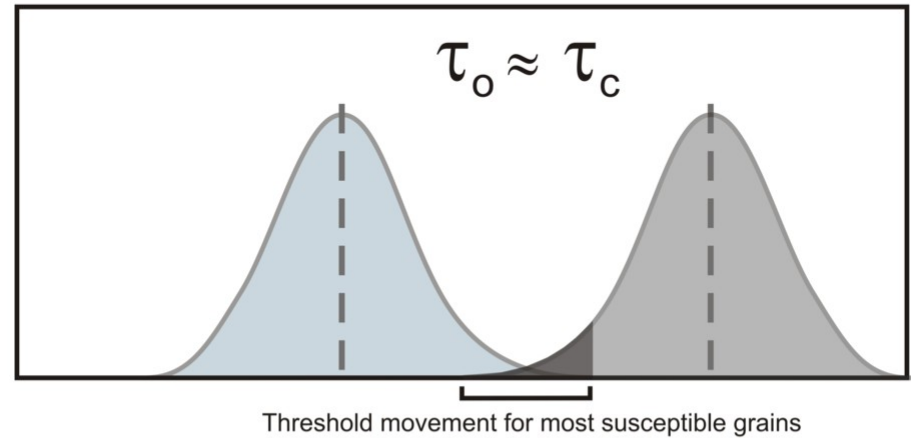
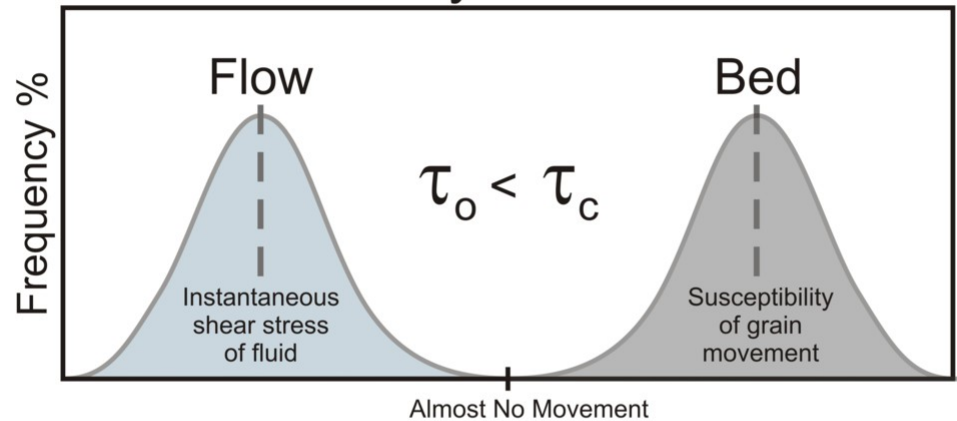


STATISTICAL
PROBLEM

Fluid Shear Stress = τ_o

Critical Shear Stress = τ_c

Probability Distributions

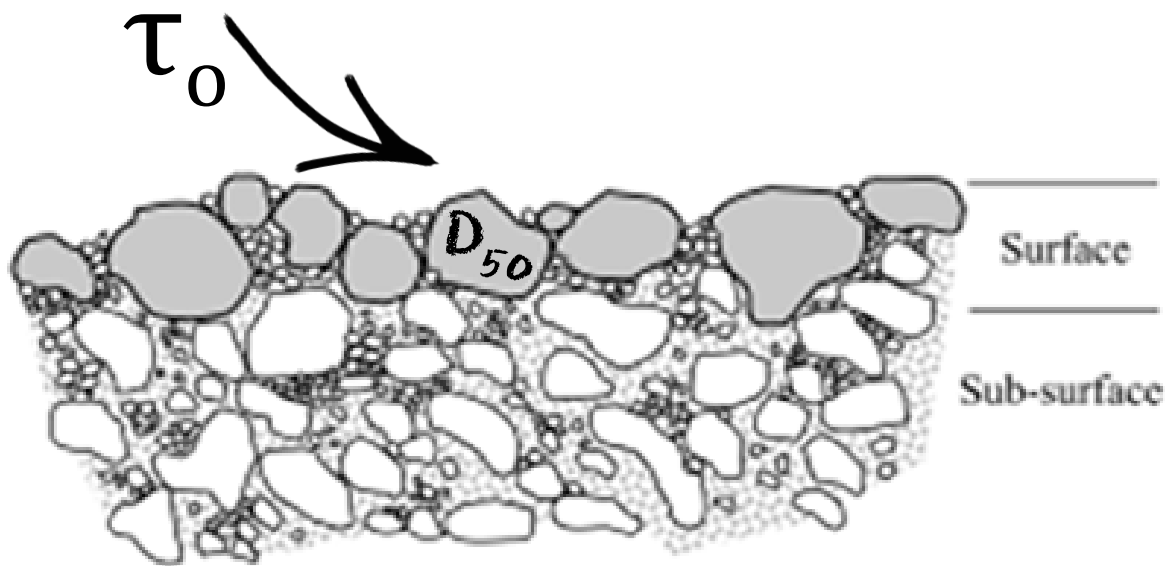


Dimensionless Shields Number

EROSION THRESHOLDS OF MOTION (SHEILDS, 1936)

$$\theta_c = \frac{\tau_c}{(\rho_s - \rho)gD_{50}}$$

Average $\theta_c = 0.045$
0.03 – 0.06
Range 0.01 to >0.1



Miller et al. 1977

Buffington and
Montgomery 1997

Also θ_c **varies** with:

Bed-State: Church 1978

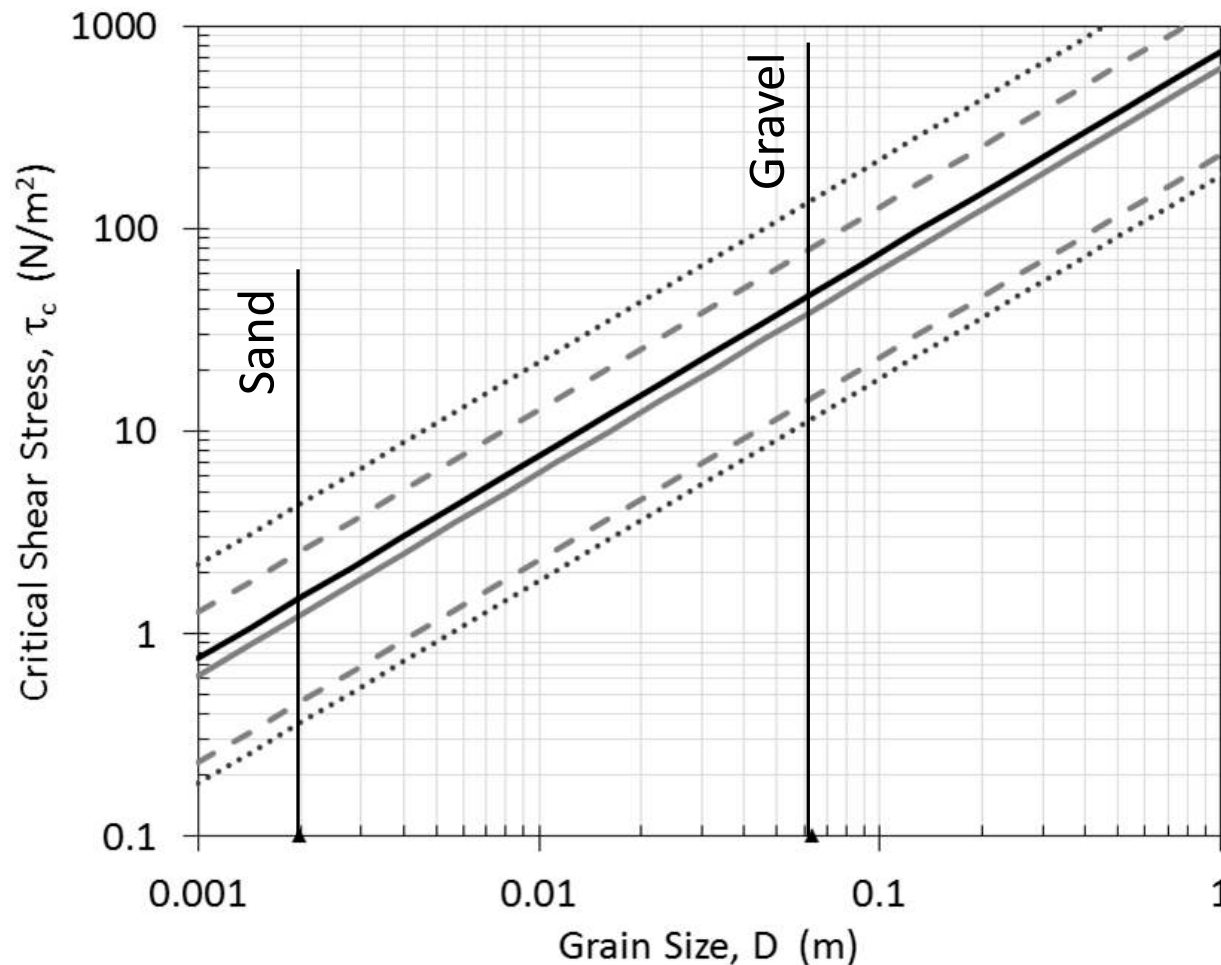
Slope: Lamb et al. 2008

Field-Measurements: Petit et al. 2015

Monte Carlo Simulation

Adapted from Stewardson and Rutherford (2008), based on data from Buffington and Montgomery (1997)

θ_c treated as a **random** variable with log-normal distribution
mean = **0.045**, standard deviation = **0.03**, $n = 1000$ (per size, D)



$$\tau_c = \theta_c (\rho_s - \rho)gD$$

Gravel = 6.4 cm

Average $\tau_c = \mathbf{48.2}$ N/m²

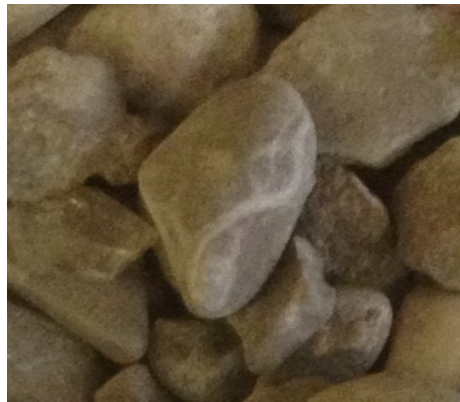
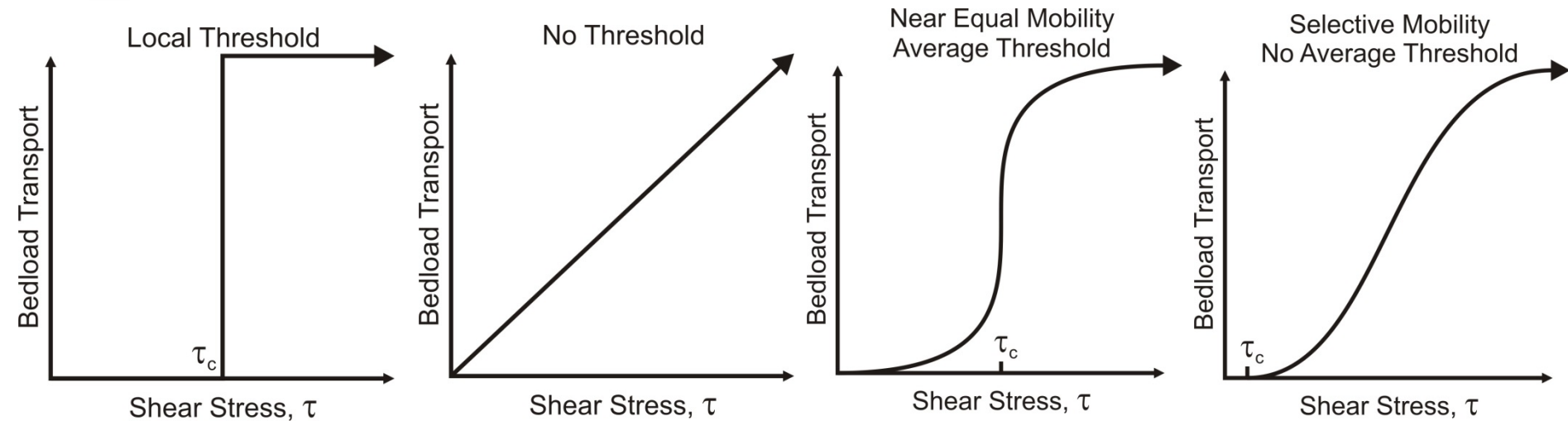
Mean's 95% Confidence
Interval: 46.2 – 50.3 N/m²

$\pm 4.5\%$

± 1 Standard Deviation
14.8 – 81.6 N/m²

95% of Data
11.7 – 140.4 N/m²

Erosion Thresholds and Scale

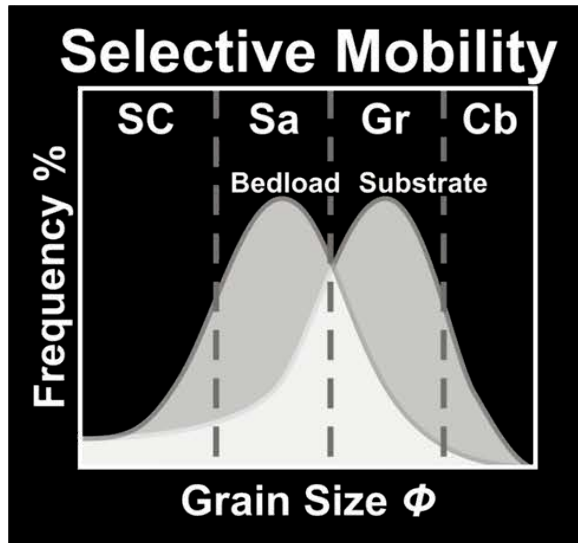
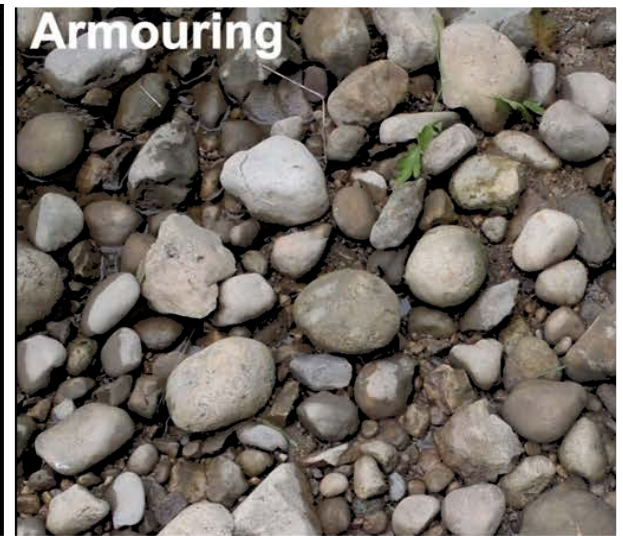
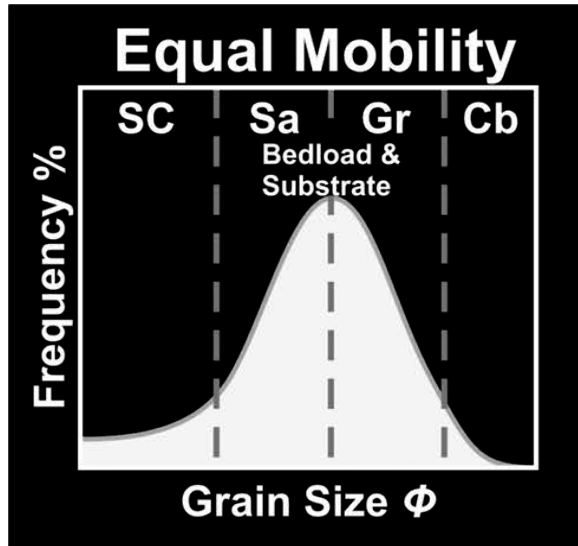


Single particle or
uniform grain-size
scale



Average Channel Scale

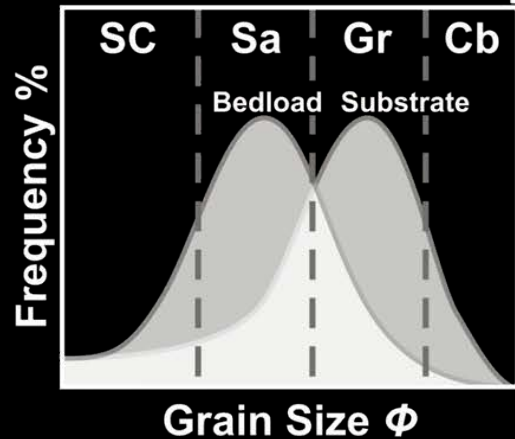
Sediment Mobility Theory



(Distribution graphs adapted from Venditti et al., In Press)

Sediment Mobility Theory

Selective Mobility



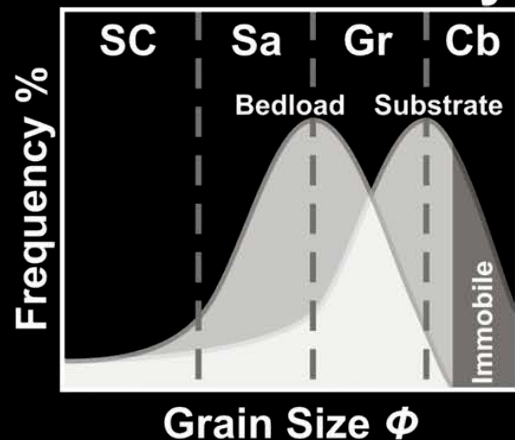
Sand and Gravel Mixtures



Sand Dominated



Partial Mobility



Cobble Dominated



Cobble and Sand Mixtures



(Distribution graphs adapted from Venditti et al., In Press)

SELECTIVE MOBILITY

HIDING FUNCTIONS

$$\theta_{ci} = a \left(\frac{D_i}{D_{50}} \right)^b$$

KOMAR (1987, 1996)

$$a = \theta_{c50} \approx 0.045$$

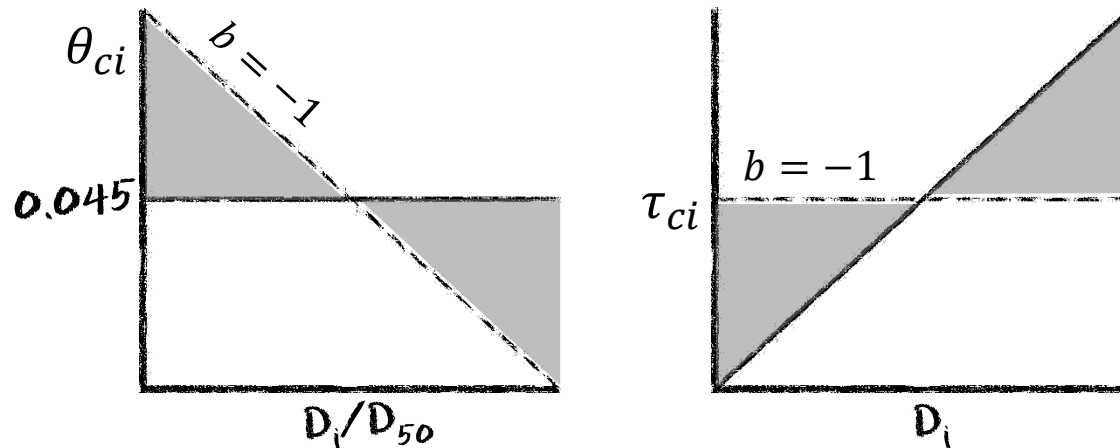
$$b = -1 \text{ Equal Mobility}$$

$$-1 < b < 0 \text{ Selective Mobility}$$

$$b \approx -0.6 \text{ Average}$$

Example:

$$\theta_{ci} = 0.0375 \left(\frac{D_i}{D_{50}} \right)^{-0.872}$$



SELECT REFERENCES

- PARKER (1990)

<http://hydrolab.illinois.edu/people/parkerg/default.asp>

- WILCOCK and CROWE (2003)

<http://www.stream.fs.fed.us/publications/bags.html>



SELECTIVE MOBILITY

HIDING FUNCTIONS

$$\theta_{ci} = \theta_{c50} \left(\frac{D_i}{D_{50}} \right)^b$$

$$\theta_{c50} = 0.021 + e^{(-20F_s)}$$

WILCOCK and
CROWE (2003)

$$b = \frac{0.67}{1 + e^{(1.5 - D_i/D_{50})}}$$

WHERE:
 F_s IS THE FRACTION
OF SAND

Fractional (selective) sediment transport of sediment mixtures

- Non-linear effect of sand on gravel transport rates
- Two-part hiding function for more sandy and less sandy gravel mixtures
- Increases θ_c for fine fractions (reducing sediment transport rates)
- Decreases θ_c for coarse fractions (increasing sediment transport rates)
- As sand content increases, sediment transport rate increases for all grain sizes

Two Different Applications

Engineered **Threshold** Channel



Entrainment **threshold** (force/area)

Forced riffles-pools and/or runs

Armouring (**equal mobility** or immobility)

Factors of **safety** for design stone sizing

River engineering:

“**Most**” channel designs, including stream restoration and **rehabilitation** in Ontario

‘Natural’ **Alluvial** Channel



Sediment **load** (mass/time)

Dynamic bed morphology

Fractional sediment transport (**selective mobility**)

Sediment **mixture** grain-size distributions

River assessment and channel design:

“Some” **natural** channel designs in Ontario

Watershed impacts, sediment **yield**

Stormwater erosion control targets

E.g., USDA

United States
Department of
Agriculture

Natural
Resources
Conservation
Service

Part 654 National Engineering Handbook

Chapter 8: Threshold Channel Design

Allowable shear stress
techniques ($\theta_c = 0.045$)

Factors of **safety**
x 1.2–1.3 (Fischenich)

Notes:
Adjustments for
mixtures

$$\theta_{ci} = 0.0834 \left(\frac{D_i}{D_{50}} \right)^{-0.872}$$

Chapter 9: Alluvial Channel Design

Stream Restoration Design



Table 8–1 General guidance for selecting the most appropriate channel design technique

Technique	Significant sediment load and movable channel boundaries	Boundary material smaller than sand size	Boundary material larger than sand size	Boundary material does not act as discrete particles	No baseflow in channel. Climate can support permanent vegetation
Allowable velocity		X			
Allowable shear stress			X		
Tractive power				X	
Grass lined/tractive stress					X
Alluvial channel design techniques	X				

Factor of Safety and Uncertainty

Stone Sizes for River Engineering

- References (e.g., **USDA**, NCHRP, AASHTO)
- Factor of **Safety** = 1.1 to 1.5
- **Common** recommendation is 1.2

Erosion Threshold Uncertainty (does it matter?)

- Threshold channel design – **depends...**
- Natural channels, alluvial channel design – **yes!**

‘Natural’ Alluvial Channels

- Equal mobility (threshold) assumptions need to be **justified**.
- **Selective** mobility to estimate sediment load
- Sediment **yield**, connectivity, land use **impact**



Field Verification of Thresholds

Field Bedload Measurements

- Tagging, tracing
- Trapping, detention
- Impact, acoustics
- Sediment budgets

Need Standard Definitions

- What measurement **technique**?
- **Threshold** stone sizes versus sediment load estimates?
- Length of **monitoring** period, quality of **hydrographs**?

Project Expectations

- **Not** standard practice, cost and schedule limitations
- Practitioners that **do** “field truthing” should be:
 - Clear about scope and **limitations**
 - Open to **Publication** and peer-review

Reliable field **truthing** is easier said than done!





Erosion Threshold Awareness

The Science and Practice

- Understand **limitations** of Shields number
- Don't be scared of **selective** mobility
- Threshold versus **alluvial** channels
- Factors of safety and **uncertainty**
- **Expectations** for Field Verification

Selective Mobility Applications

- **Sediment** load, yield, budgets, monitoring
- Stormwater management **erosion criteria**





Thank You!

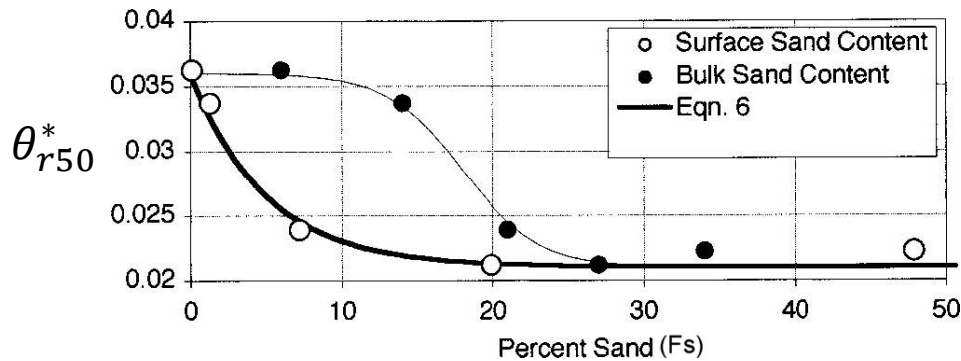
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More Wilcock and Crowe (2003)



Uses **reference** shear stress (τ_r) and **Shields** number (θ_{r50}^*)

Non-linear relation between sand content and sediment transport rates

As $F_s \uparrow$, θ_{r50}^* and $\tau_r \downarrow$ thus **increasing** sediment transport rates for all sizes

Two-part trend in hiding function relative to τ_r for single-sized sediment (1:1 line)

Hiding function acts to:

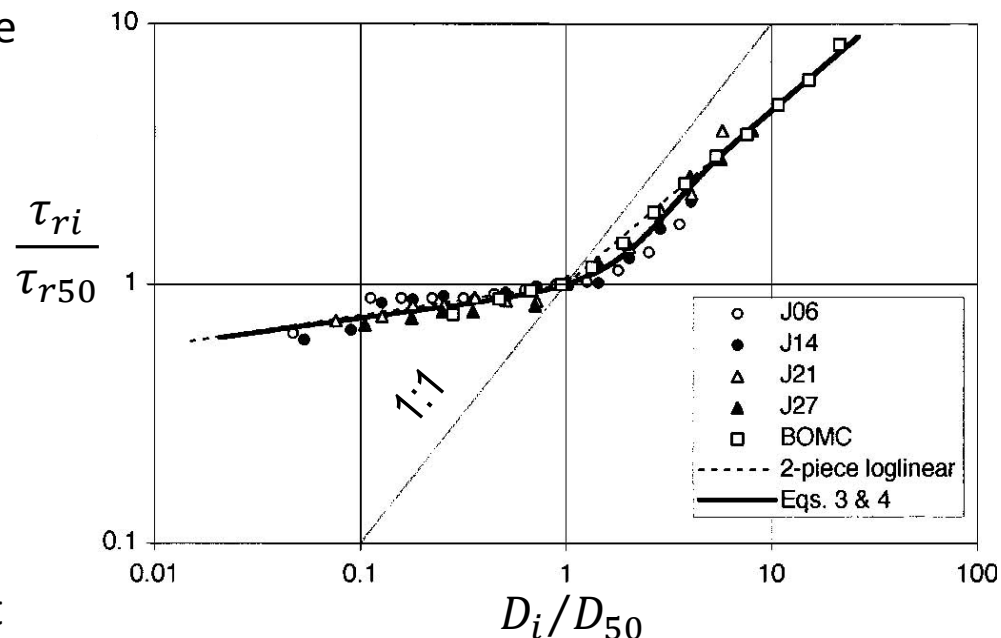
Finer fractions:

$\tau_r \uparrow$ ($\downarrow$ sediment transport)

Coarser fractions:

$\tau_r \downarrow$ ($\uparrow$ sediment transport)

*Sand **changes** gravel sediment transport



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List of References

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